

basic education

Department:
Basic Education
REPUBLIC OF SOUTH AFRICA

NATIONAL SENIOR CERTIFICATE

GRADE 12

MATHEMATICS P1

NOVEMBER 2011

MEMORANDUM

MARKS: 150

DEPARTMENT OF BASIC EDUCATION
2011 -11- 02
PRIVATE BAG X 110 PRETORIA 0001
PUBLIC EXAMINATIONS

Approved: M. H. G. -or
Approved: PMG
5/11/2011

This memorandum consists of 28 pages.

Approved: M. S. S. -or
05 November 2011

NOTE:

- If a candidate answers a question TWICE, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent Accuracy applies in all aspects of the marking memorandum.

QUESTION 1

1.1.1	$x(x+1) = 6$ $x^2 + x = 6$ $x^2 + x - 6 = 0$ $(x+3)(x-2) = 0$ $x = -3 \text{ or } 2$ <p>OR</p> $x^2 + x - 6 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $= \frac{-1 \pm \sqrt{1^2 - 4(1)(-6)}}{2(1)}$ $x = -3 \text{ or } 2$	<p>Note: Answers by inspection: award 3/3 marks</p> <p>Note: Answer only of $x = 2$: award 1/3 marks</p> <p>Note: If candidate converts equation to linear: award 0/3 marks</p>	✓ standard form ✓ factors ✓ answers (3)
	$3x^2 - 4x = 8$ $3x^2 - 4x - 8 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $= \frac{-(-4) \pm \sqrt{(-4)^2 - 4(3)(-8)}}{2(3)}$ $= \frac{4 \pm \sqrt{16 + 96}}{6}$ $= \frac{4 \pm \sqrt{112}}{6}$ $= \frac{2 \pm 2\sqrt{7}}{3}$ $= 2,43 \text{ or } -1,10$	<p>Note: If candidate uses incorrect formula: maximum 1/4 marks (for standard form)</p> <p>Note: Penalise 1 mark for inaccurate rounding off to ANY number of decimal places if candidate gives decimal answers.</p> <p>Note: If an error in subs and gets: $\frac{4 \pm \sqrt{-80}}{6}$ and states "no solution": maximum 3/4 marks If doesn't conclude with "no solution": maximum 2/4 marks</p>	✓ standard form ✓ substitution into correct formula ✓ answers (3)
1.1.2	$3x^2 - 4x = 8$ $3x^2 - 4x - 8 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $= \frac{-(-4) \pm \sqrt{(-4)^2 - 4(3)(-8)}}{2(3)}$ $= \frac{4 \pm \sqrt{16 + 96}}{6}$ $= \frac{4 \pm \sqrt{112}}{6}$ $= \frac{2 \pm 2\sqrt{7}}{3}$ $= 2,43 \text{ or } -1,10$	<p>Note: If candidate uses incorrect formula: maximum 1/4 marks (for standard form)</p> <p>Note: Penalise 1 mark for inaccurate rounding off to ANY number of decimal places if candidate gives decimal answers.</p> <p>Note: If an error in subs and gets: $\frac{4 \pm \sqrt{-80}}{6}$ and states "no solution": maximum 3/4 marks If doesn't conclude with "no solution": maximum 2/4 marks</p>	✓ standard form ✓ substitution into correct formula ✓ $\sqrt{112}$ ✓ $\frac{4 \pm \sqrt{112}}{6}$ or decimal answer (4)
			<i>MJH</i>

OR

$$\begin{aligned}
 3x^2 - 4x &= 8 \\
 3x^2 - 4x - 8 &= 0 \\
 x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \\
 &= \frac{-(-4) \pm \sqrt{(-4)^2 - 4(3)(-8)}}{2(3)} \\
 &= 2.43 \text{ or } -1.10
 \end{aligned}$$

Note: Penalise 1 mark for inaccurate rounding off to ANY number of decimal places if candidate gives decimal answers

✓ standard form

✓ substitution into correct formula

✓ answer
✓ answer

(4)

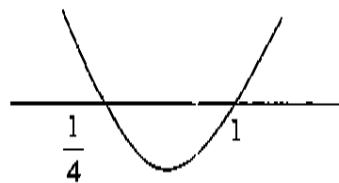
1.1.3

$$4x^2 + 1 \geq 5x$$

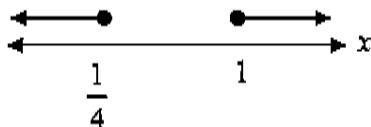
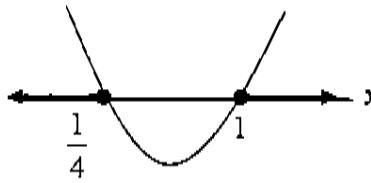
$$4x^2 - 5x + 1 \geq 0$$

$$(4x-1)(x-1) \geq 0$$

$$\begin{array}{c}
 + \quad 0 \quad - \quad 0 \quad +
 \\ \hline
 1 \quad \quad \quad 1
 \end{array}$$



$$x \leq \frac{1}{4} \text{ or } x \geq 1 \quad \text{OR} \quad \left(-\infty; \frac{1}{4}\right] \cup [1; \infty)$$

OR**OR**

Note: If candidate gives either of these correct graphical solutions but writes down the incorrect intervals or uses AND: max 3/4 marks

NOTES:

If a candidate gives an answer of $1 \leq x \leq \frac{1}{4}$ then max 3/4 marks.

If a candidate gives an answer of $\frac{1}{4} \leq x \leq 1$ then max 2/4 marks.

If a candidate gives an answer of $x \leq \frac{1}{4}$ and $x \geq 1$ then max 3/4 marks.

If the candidate leaves out the equality of the notation then penalty of 1 mark.

If a candidate gives an answer of $x \leq \frac{1}{4}; x \geq 1$ then max 3/4 marks.

If candidate gives $x \geq \frac{1}{4}$ and/or $x \geq 1$, BREAKDOWN: max 2/4 marks.

If candidate gives :
$$\begin{array}{c}
 + \quad 0 \quad - \quad 0 \quad +
 \\ \hline
 1 \quad \quad \quad 1
 \end{array}$$

award 3/4 marks

M8

PP

M1H7

1.2.1	$x^2 + 5xy + 6y^2 = 0$ $(x + 3y)(x + 2y) = 0$ $x + 3y = 0 \quad x + 2y = 0$ $x = -3y \quad \text{OR} \quad x = -2y$ $\frac{x}{y} = -3 \quad \frac{x}{y} = -2$	<p>Note: If a candidate gives $-\frac{x}{y} = 3$ or $-\frac{x}{y} = 2$ award 2/3 marks</p>	✓ factors ✓✓ answers (3)
OR	<p>Let $k = \frac{x}{y}$</p> $x^2 + 5xy + 6y^2 = 0$ $\left(\frac{x}{y}\right)^2 + 5\left(\frac{x}{y}\right) + 6 = 0$ $k^2 + 5k + 6 = 0$ $(k + 3)(k + 2) = 0$ $k = -3 \quad \text{or} \quad k = -2$ $\frac{x}{y} = -3 \quad \text{or} \quad \frac{x}{y} = -2$	✓ factors ✓✓ answers (3)	
OR	$x^2 + 5xy + 6y^2 = 0$ $x = \frac{-5y \pm \sqrt{(5y)^2 - 4(1)(6y^2)}}{2(1)}$ $x = \frac{-5y \pm \sqrt{y^2}}{2}$ $x = \frac{-5y \pm y}{2}$ $x = -3y \quad x = -2y$ $\frac{x}{y} = -3 \quad \text{or} \quad \frac{x}{y} = -2$	✓ substitutes correctly into correct formula ✓✓ answers (3)	
OR	$x^2 + 5xy + 6y^2 = 0$ $x^2 + 5xy + \left(\frac{5}{2}y\right)^2 = -6y^2 + \left(\frac{5}{2}y\right)^2$ $\left(x + \frac{5}{2}y\right)^2 = \frac{1}{4}y^2$ $x + \frac{5}{2}y = \pm \frac{1}{2}y$ $x = -\frac{5}{2}y \pm \frac{1}{2}y$	✓ completing the square	

Mathematics/PI

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$$x = -3y \quad x = -2y$$

$$\frac{x}{y} = -3 \quad \text{or} \quad \frac{x}{y} = -2$$

✓✓ answers

(3)

OR

$$\text{Let } k = \frac{x}{y}$$

$$x = ky$$

$$x^2 + 5xy + 6y^2 = 0$$

$$(ky)^2 + 5y(ky) + 6y^2 = 0$$

$$k^2y^2 + 5y^2k + 6y^2 = 0$$

$$y^2(k^2 + 5k + 6) = 0$$

$$(k^2 + 5k + 6) = 0$$

$$(k+3)(k+2) = 0$$

$$k = -3 \quad \text{or} \quad k = -2$$

$$\frac{x}{y} = -3 \quad \text{or} \quad \frac{x}{y} = -2$$

✓ factors

✓✓ answers

(3)

Note: $(x,y) = (0,0)$ is also a solution, but in this case $\frac{x}{y}$ is undefined

OR

$$\text{Let } y = 1,$$

$$x^2 + 5x + 6 = 0$$

$$(x+2)(x+3) = 0$$

$$x = -2 \quad \text{or} \quad x = -3$$

$$\frac{x}{y} = -2 \quad \text{or} \quad \frac{x}{y} = -3$$

✓ factors

✓✓ answers

(3)

1.2.2	$x + y = 8$ $-3y + y = 8$ $-2y = 8 \quad \text{OR} \quad -y = 8$ $y = -4 \quad \text{or} \quad y = -8$ $x = 12 \quad \text{or} \quad x = 16$	✓ substitution $x = -3y$ ✓ subs $x = -2y$ ✓✓ y values ✓ both x values correct (5)
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OR

$$\frac{8-y}{y} = -3 \quad \text{OR} \quad \frac{8-y}{y} = -2$$

$$8-y = -3y \quad 8-y = -2y$$

$$8 = -2y \quad 8 = -y$$

$$y = -4 \quad y = -8$$

$$x = 12 \quad x = 16$$

✓ $x = 8 - y$

✓ substitution

✓✓ y values✓ both correct x values

(5)

OR $x + y = 8$ $y = 8 - x$ $\frac{x}{8-x} = -3 \quad \text{OR} \quad \frac{x}{8-x} = -2$ $x = -3(8-x) \quad x = -2(8-x)$ $x = -24 + 3x \quad x = -16 + 2x$ $-2x = -24 \quad -x = -16$ $x = 12 \quad x = 16$ $y = -4 \quad y = -8$	✓ $y = 8 - x$ ✓ substitution ✓✓ x values correct ✓ both y values correct (5)
OR $(x+2y)(x+3y) = 0$ $x + y = 8$ $x = 8 - y$ $(y+8)(2y+8) = 0$ $y = -8 \text{ or } y = -4$ $x = 16 \quad x = 12$	✓ $x = 8 - y$ ✓ substitution ✓✓ y values correct ✓ both x values correct (5)
OR $x = 8 - y$ $(8-y)^2 + 5(8-y)y + 6y^2 = 0$ $64 - 16y + y^2 + 40y - 5y^2 + 6y^2 = 0$ $2y^2 + 24y + 64 = 0$ $y^2 + 12y + 32 = 0$ $(y+8)(y+4) = 0$ $y = -8 \text{ or } y = -4$ $x = 16 \quad x = 12$	✓ $x = 8 - y$ ✓ substitution ✓ factors ✓ both y values correct ✓ both x values correct (5)

OR

$$x = 8 - y$$

$$(8 - y)^2 + 5(8 - y)y + 6y^2 = 0$$

$$64 - 16y + y^2 + 40y - 5y^2 + 6y^2 = 0$$

$$2y^2 + 24y + 64 = 0$$

$$y^2 + 12y + 32 = 0$$

$$y = \frac{-12 \pm \sqrt{12^2 - 4(1)(32)}}{2(1)}$$

$$= \frac{-12 \pm \sqrt{16}}{2}$$

$$y = -8 \text{ or } y = -4$$

$$x = 16 \quad x = 12$$

Note:

If a candidate uses the formula and replaces x for y and then answers are swapped:
maximum 4/5 marks

✓ $x = 8 - y$

✓ substitution

✓ substitutes into
correct formula

✓ both y values
correct

✓ both x values
correct

(5)

OR

$$y = 8 - x$$

$$x^2 + 5x(8 - x) + 6(8 - x)^2 = 0$$

$$x^2 + 40x - 5x^2 + 6(64 - 16x + x^2) = 0$$

$$2x^2 - 56x + 384 = 0$$

$$x^2 - 28x + 192 = 0$$

$$(x - 16)(x - 12) = 0$$

$$x = 12 \quad x = 16$$

$$y = -4 \quad y = -8$$

✓ $y = 8 - x$

✓ substitution

✓ factors

✓ both x values
correct

✓ both y values
correct

(5)

OR

$$y = 8 - x$$

$$x^2 + 5x(8 - x) + 6(8 - x)^2 = 0$$

$$x^2 + 40x - 5x^2 + 6(64 - 16x + x^2) = 0$$

$$2x^2 - 56x + 384 = 0$$

$$x^2 - 28x + 192 = 0$$

$$x = \frac{-(-28) \pm \sqrt{(-28)^2 - 4(1)(192)}}{2(1)}$$

$$= \frac{28 \pm \sqrt{416}}{2}$$

$$x = 12 \quad x = 16$$

$$y = -4 \quad y = -8$$

✓ $y = 8 - x$

✓ substitution

✓ substitutes into
correct formula

✓ both x values
correct

✓ both correct y
values

(5)

[Signature] [19]

QUESTION 2

2.1.1	$\begin{aligned}x - 4 &= 32 - x \\2x &= 36 \\x &= 18\end{aligned}$ <p>OR</p> $\begin{aligned}a &= 4 \\a + 2d &= 32 \\2d &= 28 \\d &= 14 \\x &= 14 + 4 \\x &= 18\end{aligned}$ <p>OR</p> $x = \frac{4 + 32}{2} = 18$	<p>Note: If answer only: award 2/2 marks</p> <p>Note: If candidate writes $x - 4 = 32 - x$ only (i.e. omits equality): 0/2 marks</p>	$\checkmark T_2 - T_1 = T_3 - T_2$ \checkmark answer (2) $\checkmark a + 2d = 32$ and $a = 4$ \checkmark answer (2) \checkmark substitutes correctly into arithmetic mean formula i.e. $\frac{4+32}{2}$ \checkmark answers (2)
2.1.2	$\begin{aligned}\frac{x}{4} &= \frac{32}{x} \\x^2 &= 128 \\x &= \pm\sqrt{128} \\x &= \pm 8\sqrt{2} \quad \text{OR} \quad x = \pm 11,31 \quad \text{OR} \quad x = \pm 2^{\frac{7}{2}}\end{aligned}$ <p>OR</p> $\begin{aligned}a &= 4 \\r &= \frac{x}{4} \\ar^2 &= 4\left(\frac{x}{4}\right)^2 \\32 &= 4\left(\frac{x}{4}\right)^2 \\x^2 &= 128 \\x &= \pm\sqrt{128} \\x &= \pm 8\sqrt{2} \quad \text{or} \quad x = \pm 11,31 \quad \text{or} \quad x = \pm 2^{\frac{7}{2}}\end{aligned}$ <p>OR</p> $\begin{aligned}x &= \pm\sqrt{4 \times 32} \\x &= \pm\sqrt{128} \quad \text{or} \quad x = \pm 8\sqrt{2} \quad \text{or} \quad x = \pm 11,31 \quad \text{or} \quad x = \pm 2^{\frac{7}{2}}\end{aligned}$	<p>Note: If candidate writes $\frac{x}{4} = \frac{32}{x}$ only (i.e. omits equality): 0/2 marks</p> <p>Note: If only $x = \sqrt{128}$ then penalty 1 mark</p>	$\checkmark \frac{T_2}{T_1} = \frac{T_3}{T_2}$ $\checkmark x^2 = 128$ \checkmark both answers (surd or decimal or exponential form) (3) $\checkmark 32 = 4\left(\frac{x}{4}\right)^2$ $\checkmark x^2 = 128$ \checkmark both answers (surd or decimal or exponential form) (3) $\checkmark \checkmark$ substitutes correctly into geometric mean formula i.e. $\pm\sqrt{4 \times 32}$ \checkmark both answers (surd or decimal or exponential form) (3)

2.2	$ \begin{aligned} P &= \sum_{k=1}^{13} 3^{k-5} \\ &= 3^{1-5} + 3^{2-5} + 3^{3-5} + \dots + 3^{13-5} \\ &= 3^{-4} + 3^{-3} + 3^{-2} + \dots + 3^8 \\ &= \frac{3^{-4}(3^{13} - 1)}{3 - 1} \\ &= 9841,49 \quad \text{or} \quad 9841\frac{40}{81} \quad \text{or} \quad \frac{797161}{81} \end{aligned} $ <p>Note: Correct answer only: 1/4 marks only</p>	<ul style="list-style-type: none"> ✓ $a = 3^{-4}$ or $\frac{1}{81}$ ✓ $r = 3$ ✓ subs into correct formula ✓ answer <p>(4)</p>
OR	$ \begin{aligned} P &= \sum_{k=1}^{13} 3^{k-5} \\ &= 3^{1-5} + 3^{2-5} + 3^{3-5} + \dots + 3^{13-5} \\ &= 3^{-4} + 3^{-3} + 3^{-2} + \dots + 3^8 \\ &= \frac{1}{81} + \frac{1}{27} + \frac{1}{9} + \dots + 6561 \\ &= 9841,49 \quad \text{or} \quad 9841\frac{40}{81} \quad \text{or} \quad \frac{797161}{81} \end{aligned} $ <p>Note: If the candidate rounds off and gets 9841,46 (i.e. correct to one decimal place): DO NOT penalise for the rounding off.</p>	<ul style="list-style-type: none"> ✓✓ expand the sum ✓ 13 terms in expansion ✓ answer <p>(4)</p>
2.3	$ \begin{aligned} S_n &= a + [a+d] + [a+2d] + \dots + [a+(n-2)d] + [a+(n-1)d] \\ S_n &= [a+(n-1)d] + [a+(n-2)d] + \dots + [a+d] + a \\ 2S_n &= [2a+(n-1)d] + [2a+(n-1)d] + \dots + [2a+(n-1)d] + [2a+(n-1)d] \\ &= n[2a+(n-1)d] \\ S_n &= \frac{n}{2}[2a+(n-1)d] \end{aligned} $	<ul style="list-style-type: none"> ✓ writing out S_n ✓ "reversing" S_n ✓ expressing $2S_n$ ✓ grouping to get $2S_n = n[2a+(n-1)d]$ <p>(4)</p>
OR	$ \begin{aligned} S_n &= a + [a+d] + [a+2d] + \dots + (T_n - d) + T_n \\ S_n &= T_n + (T_n - d) + \dots + [a+d] + a \\ 2S_n &= a + T_n + a + T_n + a + T_n + \dots + a + T_n \\ &= n[a + a + (n-1)d] \\ &= [2a + (n-1)d] \\ S_n &= \frac{n}{2}[2a + (n-1)d] \end{aligned} $ <p>Note: If a candidate uses a circular argument (eg $S_{n+1} = S_n + T_n$): max 1/4 marks (for writing out S_n)</p>	<ul style="list-style-type: none"> ✓ writing out S_n ✓ "reversing" S_n ✓ expressing $2S_n$ ✓ grouping to get $2S_n = n[a + a + (n-1)d]$ <p>(4)</p>
	<p>Note: If a candidate uses a specific linear sequence, then NO marks.</p>	[13]

QUESTION 3

3.1	21; 24	Note: If candidate writes $T_8 = 21$ $T_7 = 24$: award 1/2 marks	✓ 21 ✓ 24 (2)
3.2	$T_{2k} = 3 \cdot 2^{k-1}$ and so $T_{52} = 3 \cdot 2^{26-1} = 100663296$ $T_{2k-1} = 3 + 6(k-1) = 6k - 3$ and so $T_{51} = 6(26) - 3 = 153$ $T_{52} - T_{51} = 100663296 - 153 \\ = 100663143$ <p>OR</p> <p>Consider sequence P: 3 ; 6 ; 12 ... $P_n = 3 \cdot 2^{n-1}$ $P_{26} = 3 \cdot 2^{26-1} = 100663296$</p> <p>Consider sequence Q: 3 ; 9 ; 15 ... $Q_n = 6n - 3$ $Q_{26} = 6(26) - 3 = 153$ $T_{52} - T_{51} = P_{26} - Q_{26} \\ = 100663296 - 153 \\ = 100663143$</p>	Note: If candidate writes out all 52 terms and gets correct answer: award 5/5 marks Note: If candidate used $k = 52$: max 2/5 Note: if candidate interchanges order i.e. does $T_{51} - T_{52}$: max 4/5 marks Note: writes out all 52 terms and subtracts $T_{51} - T_{52}$: max 4/5 marks	✓ $3 \cdot 2^{k-1}$ ✓ T_{52} ✓ $6k - 3$ ✓ T_{51} ✓ answer ✓ $P_n = 3 \cdot 2^{n-1}$ ✓ P_{26} ✓ $Q_n = 6n - 3$ ✓ Q_{26} ✓ answer (5)

Please turn over

3.3	<p>For all $n \in \mathbb{N}$, $n = 2k$ or $n = 2k - 1$ for some $k \in \mathbb{N}$</p> <p>If $n = 2k$:</p> $T_n = T_{2k} = 3 \cdot 2^{k-1}$ <p>If $n = 2k - 1$:</p> $\begin{aligned} T_n &= T_{2k-1} \\ &= 6k - 3 \\ &= 3(2k - 1) \end{aligned}$ <p>In either case, T_n has a factor of 3, so is divisible by 3.</p> <p>Note: If a candidate only illustrates divisibility by 3 with a specific finite part of the sequence, not the general term: 0/2 marks</p>	<p>✓ factors $3 \cdot 2^{k-1}$</p> <p>✓ factors $3(2k - 1)$</p> <p>(2)</p> <p>✓ factors $3 \cdot 2^{n-1}$</p> <p>✓ factors $3(2n - 1)$</p> <p>(2)</p> <p>✓ odd multiples of 3 ✓ 3 times a power of 2</p> <p>(2)</p> <p>[9]</p>
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QUESTION 4

4.1 The second, third, fourth and fifth terms are 1 ; -6 ; T_4 and -14

First differences are: -7 ; $T_4 + 6$; -14 - T_4

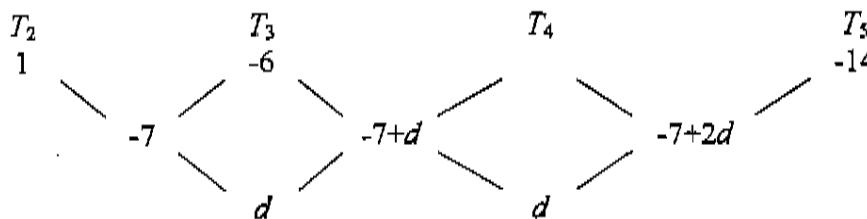
So $T_4 + 6 + 7 = -14 - 2T_4 - 6$.

$$T_4 = -11$$

$$d = -11 + 6 + 7 = 2 \quad \text{or} \quad -14 + 22 - 6 = 2$$

Note: Answer only (i.e.
 $d = 2$) with no working:
3 marks

OR



$$T_5 - T_2 = (T_5 - T_4) + (T_4 - T_3) + (T_3 - T_2)$$

$$-15 = (-7 + 2d) + (-7 + d) + -7$$

$$-15 = -21 + 3d$$

$$6 = 3d$$

$$d = 2$$

Note: Candidate uses trial
and error and shows this:
award 5/5 marks

- ✓ -7
- ✓ $T_4 + 6$
- ✓ -14 - T_4

- ✓ setting up
equation

$$T_5 - T_2 = (T_5 - T_4) + (T_4 - T_3) + (T_3 - T_2)$$

- ✓ answer

(5)

- ✓ -7
- ✓ -7 + d
- ✓ -7 + 2d

- ✓ setting up
equation

$$T_5 - T_2 = (T_5 - T_4) + (T_4 - T_3) + (T_3 - T_2)$$

- ✓ answer

(5)

OR

$$4a + 2b + c = 1$$

$$9a + 3b + c = -6$$

$$5a + b = -7$$

- ✓ $4a + 2b + c = 1$
- ✓ $9a + 3b + c = -6$

$$25a + 5b + c = -14$$

$$16a + 2b = -8$$

$$10a + 2b = -14$$

$$6a = 6$$

$$a = 1$$

$$d = 2a = 2$$

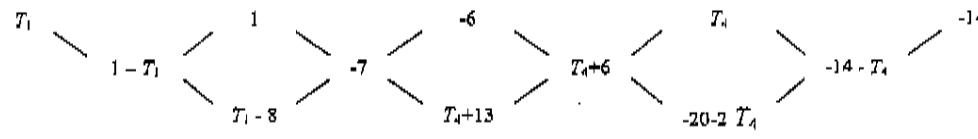
$$\checkmark 25a + 5b + c = -14$$

- ✓ solved
simultaneously

- ✓ answer

(5)

OR



$$T_4 + 13 = -20 - 2T_4$$

$$3T_4 = -33$$

$$T_4 = -11$$

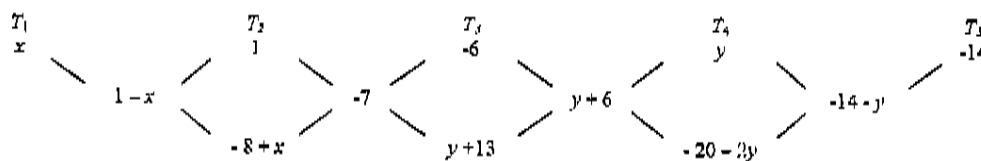
$$d = -11 + 13$$

$$d = 2$$

- ✓ -7
- ✓ $T_4 + 6$
- ✓ -14 - T_4

- ✓ setting up
equation
- ✓ answer

(5)

OR

$$y + 13 = -20 - 2y$$

$$3y = -33$$

$$y = -11$$

- ✓ - 7
- ✓ $y + 6$
- ✓ $-14 - y$

- ✓ setting up equation
- ✓ answer

(5)

$$\text{Second difference} = y + 13 = -11 + 13 = 2$$

4.2	T_1 1 -6 \ / \ / -9 -7 \ / \ / 2	Note: Answer only: award 2/2 marks	✓ method ✓ $T_1 = 10$
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$$T_1 = 10$$

OR

$$a = 1$$

$$5a + b = -7$$

$$5(1) + b = -7$$

$$b = -12$$

$$a + b + c = 1$$

$$4(1) + 2(-12) + c = 1$$

$$c = 21$$

$$T_n = n^2 - 12n + 21$$

$$T_1 = (1)^2 - 12(1) + 21 \\ = 10$$

Note:
If incorrect d in 4.1,
2/2 CA marks for
 $T_1 = d + 8$ (since
 $1 - T_1 = -7 - d$)

- ✓ method

- ✓ $T_1 = 10$

(2)

OR

$$T_4 + 13 = -8 + T_1$$

$$y + 13 = -8 + x$$

- ✓ method

$$-11 + 13 = -8 + T_1 \quad \text{OR} \quad -11 + 13 = -8 + x$$

$$T_1 = 10$$

$$x = 10$$

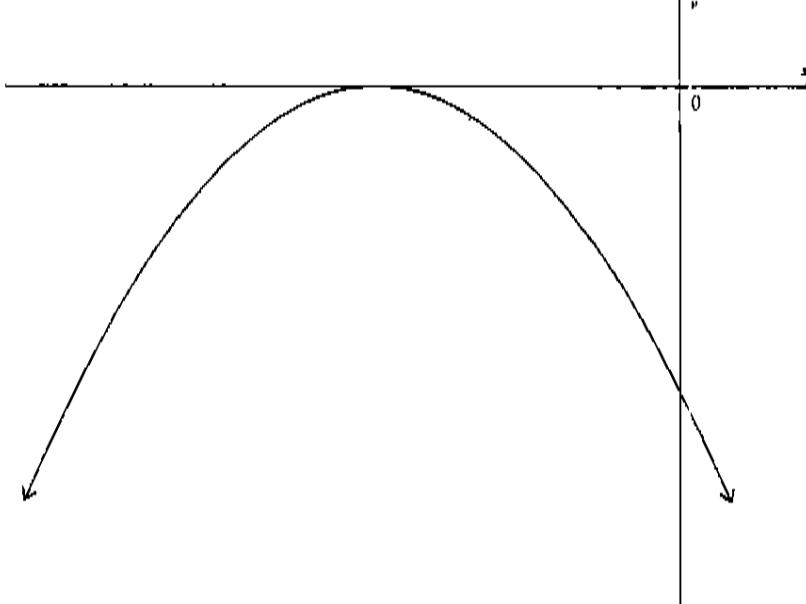
- ✓ $T_1 = 10$

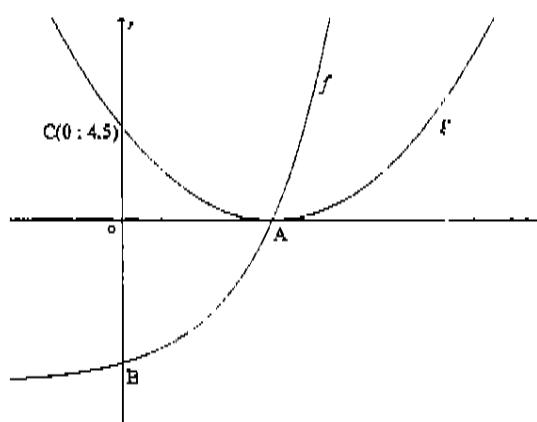
(2)

[7]

QUESTION 5

5.1.1	$\begin{aligned} y &= f(0) \\ &= \frac{-6}{0-3} - 1 \\ &= 1 \end{aligned}$ <p>$(0 ; 1)$ OR $x = 0$ and $y = 1$</p>	<p>Note: Mark 5.1.1 and 5.1.2 as a single question. If the intercepts are interchanged: max 3/5 marks</p>	✓ $y = 1$ ✓ $x = 0$ (2)
5.1.2	$\begin{aligned} 0 &= \frac{-6}{x-3} - 1 \\ 1 &= \frac{-6}{x-3} \\ x-3 &= -6 \\ x &= -3 \\ (-3 ; 0) \end{aligned}$		✓ $y = 0$ ✓ $x-3 = -6$ ✓ answer (3)
5.1.3	<p>The graph shows a rational function with a vertical asymptote at $x = 3$ and a horizontal asymptote at $y = -1$. The curve passes through the points $(-3, 0)$ and $(0, 1)$.</p>	<p>Note: The graph must tend towards the asymptotes in order to be awarded the shape mark</p>	✓ shape ✓ both intercepts correct ✓ horizontal asymptote ✓ vertical asymptote (4)
5.1.4	$-3 < x < 3$ OR $(-3 ; 3)$ OR $-3 < x$ and $x < 3$	<p>Note: if candidate writes $-3 < x$ only: 1/2 marks</p> <p>Note: if candidate writes $x < 3$ only: 1/2 marks</p>	✓ -3 and 3 ✓ inequality OR interval notation (2)

5.1.5	$y = \frac{-6}{-2-3} - 1$ $= \frac{1}{5}$ $m = \frac{1 - \frac{1}{5}}{0 - (-2)}$ $= \frac{2}{5}$ <p>OR</p> $m = \frac{f(0) - f(-2)}{0 - (-2)}$ $= \frac{1 - \frac{1}{5}}{0 + 2}$ $= \frac{2}{5}$	✓ $\frac{1}{5}$ ✓ formula ✓ substitution ✓ answer (4)
5.2	$x = -\frac{b}{2a} < 0$ since $b < 0$ and $a < 0$ 	✓ y -intercept negative ✓ turning point on the x axis ✓ turning point on the left of the y axis ✓ maximum TP and quadratic shape (4) [19]

QUESTION 6

6.1	$0 = 2^x - 8$ $8 = 2^x$ $2^3 = 2^x$ $x = 3$ $A(3 ; 0)$	$f(0) = 2^0 - 8$ $= 1 - 8$ $= -7$ $B(0 ; -7)$	✓ $y = 0$ ✓ answer for A ✓ $x = 0$ ✓ answer for B (4)
6.2	$y = -8$ OR $y + 8 = 0$	Note: no CA marks	✓ answer (1)
6.3	$h(x) = f(2x) + 8$ $= (2^{2x} - 8) + 8$ $= 4^x \text{ or } 2^{2x}$	Note: answer only: award 2/2 marks	✓ $(2^{2x} - 8)$ ✓ answer of $h(x) = 4^x \text{ or } 2^{2x}$ (2)
6.4	$x = 4^y \quad \text{OR} \quad x = 2^{2y}$ $y = \log_4 x \quad \text{OR} \quad 2y = \log_2 x$ $y = \frac{1}{2} \log_2 x \quad \text{OR} \quad y = \log_2 \sqrt{x}$ OR $y = \frac{\log x}{\log 4}$	Note: answer only award 2/2 marks Note: candidate works out f^{-1} and gets $y = \log_2(x+8)$ award 1/2 marks	✓ switch x and y ✓ answer in the form $y = \dots$ (2)
6.5	$p(x) = -\log_4 x \quad \text{OR} \quad p(x) = \log_{\frac{1}{4}} x$ OR $p(x) = \log_4 \frac{1}{x} \quad \text{OR} \quad p(x) = -\frac{1}{2} \log_2 x$ OR $y = -\log_2 \sqrt{x}$		✓ answer (1)

6.6 $\sum_{k=0}^3 g(k) - \sum_{k=4}^5 g(k)$

$$= g(0) + g(1) + g(2) + g(3) - g(4) - g(5)$$

$x = 3$ is the axis of symmetry of g

∴ by symmetry

$$g(2) = g(4) \text{ and } g(1) = g(5)$$

$$\text{Answer} = g(0) + g(3)$$

$$= 4,5 + 0$$

$$= 4,5$$

✓ $= g(0) + g(1) + g(2) + g(3) - g(4) - g(5)$

✓ $g(2) = g(4)$ and $g(1) = g(5)$

✓ $g(0) + g(3)$

✓ answer

(4)

OR

$$\sum_{k=0}^3 g(k) - \sum_{k=4}^5 g(k)$$

✓ expansion

$$\sum_{k=0}^3 g(k) = g(0) + g(1) + g(2) + g(3)$$

$$\sum_{k=4}^5 g(k) = g(4) + g(5)$$

$x = 3$ is the axis of symmetry of g

∴ by symmetry

$$g(4) = g(2)$$

✓ $g(2) = g(4)$ and $g(1) = g(5)$

$$g(5) = g(1)$$

$$\sum_{k=0}^3 g(k) - \sum_{k=4}^5 g(k)$$

✓ $g(0) + g(3)$

$$= g(0) + g(3)$$

$$= 4,5 + 0$$

✓ answer

$$= 4,5$$

(4)

OR

$$g(x) = a(x - 3)^2 + 0$$

$$4,5 = a(0 - 3)^2 + 0$$

$$4,5 = 9a$$

$$a = \frac{1}{2}$$

$$g(x) = \frac{1}{2}(x - 3)^2$$

✓ $g(x) = \frac{1}{2}(x - 3)^2$

$$\sum_{k=0}^3 g(k) - \sum_{k=4}^5 g(k)$$

$$\sum_{k=0}^3 g(k) = g(0) + g(1) + g(2) + g(3)$$

$$= 4,5 + 2 + 0,5 + 0$$

$$= 7$$

✓ expansion

11/11/11

PP

$$\sum_{k=4}^5 g(k) = g(4) + g(5)$$

$$= 0,5 + 2$$

$$= 2,5$$

$$\sum_{k=0}^3 g(k) - \sum_{k=4}^5 g(k)$$

$$= 7 - 2,5$$

$$= 4,5$$

$$\checkmark 7 - 2,5$$

\checkmark answer

(4)

OR

$$g(x) = ax^2 + bx + c$$

$$g(k) = ak^2 + bk + c$$

$$g(0) = c$$

$$g(1) = a + b + c$$

$$g(2) = 4a + 2b + c$$

$$g(3) = 9a + 3b + c$$

$$\sum_{k=0}^3 g(k) = 14a + 6b + 4c$$

$$g(4) = 16a + 4b + c$$

$$g(5) = 25a + 9b + c$$

$$\sum_{k=4}^5 g(k) = 41a + 9b + 2c$$

$$\sum_{k=0}^3 g(k) - \sum_{k=4}^5 g(k) = -27a - 3b + 2c$$

$$\checkmark \checkmark - 27a - 3b + 2c$$

$$g(x) = a(x - 3)^2 + 0$$

$$4,5 = a(0 - 3)^2 + 0$$

$$4,5 = 9a$$

$$a = \frac{1}{2}$$

$$g(x) = \frac{1}{2}(x - 3)^2$$

$$= \frac{1}{2}x^2 - 3x + \frac{9}{2}$$

$$\sum_{k=0}^3 g(k) - \sum_{k=4}^5 g(k) = -27a - 3b + 2c$$

$$\checkmark g(x) = \frac{1}{2}(x - 3)^2$$

$$= -27\left(\frac{1}{2}\right) - 3(-3) + 2\left(\frac{9}{2}\right)$$

$$= 4,5$$

\checkmark answer

M *PP* (4)
G/H/A [14]

QUESTION 7

<p>7.1</p> $A = P(1 - i)^n$ $\frac{P}{2} = P(1 - 0,07)^n$ $\frac{1}{2} = 0,93^n$ $\log \frac{1}{2} = n \log 0,93$ $n = \frac{\log \frac{1}{2}}{\log 0,93}$ $= 9,55 \text{ years}$	<p>OR</p> $A = P(1 - i)^n$ $\frac{P}{2} = P(1 - 0,07)^n$ $\frac{1}{2} = 0,93^n$ $\log_{0,93} \frac{1}{2} = n$ $n = 9,55 \text{ years}$	<p>✓ $A = \frac{P}{2}$</p> <p>✓ subs into correct formula</p> <p>✓ log</p> <p>✓ answer</p>
<p>Note: If candidate interchanges A and P i.e. uses $P = \frac{A}{2}$: max 2/4 marks</p>	<p>Note: If candidate uses incorrect formula: max 1/4 marks for $A = \frac{P}{2}$</p>	

(4)

7.2	<p>Radesh:</p> $A = P(1+in)$ $= 6000(1+0,085 \times 5) \quad \text{OR}$ $= 8550$ $A = 6000 + 8,5\% \text{ of } 6000 \times 5$ $= 6000 + 510 \times 5$ $= 6000 + 2550$ $= 8550$	$\checkmark 8550$
	$\text{Bonus} = 0,05 \times 6000$ $= 300$	
	$\text{Received} = 8550 + 300$ $= R8850$	$\checkmark R8850$
	<p>Thandi:</p> $A = P(1+i)^n$ $= 6000 \left(1 + \frac{0,08}{4}\right)^{20}$ $= R8915,68$	$\checkmark n = 20$ $\checkmark i = \frac{0,08}{4}$ $\checkmark \text{answer}$
	<p>Thandi's investment is bigger.</p>	$\checkmark \text{choice made}$
(6)		
7.3	$F_v = \text{initial deposit with interest} + \text{annuity}$ $= 1000 \left(1 + \frac{0,15}{12}\right)^{18} + 700 \left(\frac{\left(1 + \frac{0,15}{12}\right)^{18} - 1}{\frac{0,15}{12}} \right)$ $= 1250,58 + 14032,33$ $= R15282,91$	$\checkmark i = \frac{0,15}{12} \text{ or } \frac{1}{80} \text{ or } 0,0125$ $\checkmark n = 18$ $\checkmark n = 18$ $\checkmark 1000 \left(1 + \frac{0,15}{12}\right)^{18}$ $\checkmark 700 \left(\frac{\left(1 + \frac{0,15}{12}\right)^{18} - 1}{\frac{0,15}{12}} \right)$
OR		$\checkmark \text{answer}$
(6)		
	$F_v = \text{initial deposit with interest} + \text{annuity}$ $= 1000 \left(1 + \frac{0,15}{12}\right)^{18} + 700 \left(\frac{1 - \left(1 + \frac{0,15}{12}\right)^{-18}}{\frac{0,15}{12}} \right) \left(1 + \frac{0,15}{12}\right)^{18}$ $= 1250,58 + 11220,68 \left(1 + \frac{0,15}{12}\right)^{18}$ $= 1250,58 + 14032,33$ $= R15282,91$	$\checkmark i = \frac{0,15}{12} \text{ or } \frac{1}{80} \text{ or } 0,0125$ $\checkmark n = 18$ $\checkmark n = 18$ $\checkmark 1000 \left(1 + \frac{0,15}{12}\right)^{18}$ $\checkmark 700 \left(\frac{1 - \left(1 + \frac{0,15}{12}\right)^{-18}}{\frac{0,15}{12}} \right) \left(1 + \frac{0,15}{12}\right)^{18}$ $\checkmark \text{answer}$
(6)		

OR

$$F_v = 300 \left(1 + \frac{0,15}{12}\right)^{18} + 700 \left(\frac{\left(1 + \frac{0,15}{12}\right)^{19} - 1}{\frac{0,15}{12}} \right)$$

$$= 375,17 + 14\ 907,74$$

$$= \text{R}15\ 282,91$$

- ✓ $i = \frac{0,15}{12}$ or $\frac{1}{80}$ or 0,0125
- ✓ $n = 19$ (corresponding to 700)
- ✓ $n = 18$ (corresponding to 300)
- ✓ $300 \left(1 + \frac{0,15}{12}\right)^{18}$
- ✓ $700 \left(\frac{\left(1 + \frac{0,15}{12}\right)^{19} - 1}{\frac{0,15}{12}} \right)$
- ✓ answer

(6)

[16]

QUESTION 8

8.1

$$\begin{aligned} f'(x) &= \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} \\ &= \lim_{h \rightarrow 0} \frac{-4(x+h)^2 - (-4x^2)}{h} \\ &= \lim_{h \rightarrow 0} \frac{-4(x^2 + 2xh + h^2) + 4x^2}{h} \\ &= \lim_{h \rightarrow 0} \frac{-4x^2 - 8xh - 4h^2 + 4x^2}{h} \\ &= \lim_{h \rightarrow 0} \frac{-8xh - 4h^2}{h} \\ &= \lim_{h \rightarrow 0} \frac{h(-8x - 4h)}{h} \\ &= \lim_{h \rightarrow 0} (-8x - 4h) \\ &= -8x \end{aligned}$$

Note:
Incorrect notation:
no lim written:

penalty 2 marks

lim written before
equals sign:
penalty 1 mark

Note:
A candidate who
gives $-8x$ only:
0/5 marks

Note:
A candidate who omits
brackets in the line
 $\lim_{h \rightarrow 0} (-8x - 4h)$:
NO penalty

- ✓ formula
- ✓ substitution
- ✓ expansion

✓ $-8x - 4h$
✓ answer

(5)

OR

	$f(x) = -4x^2$ $f(x+h) = -4(x+h)^2$ $= -4x^2 - 8xh - 4h^2$ $f(x+h) - f(x) = -8xh - 4h^2$ $f'(x) = \lim_{h \rightarrow 0} \frac{-8xh - 4h^2}{h}$ $= \lim_{h \rightarrow 0} \frac{h(-8x - 4h)}{h}$ $= \lim_{h \rightarrow 0} (-8x - 4h)$ $= -8x$	✓ substitution ✓ expansion ✓ formula ✓ $-8x - 4h$ ✓ answer (5)
8.2.1	$y = \frac{3}{2x} - \frac{x^2}{2}$ $= \frac{3}{2}x^{-1} - \frac{1}{2}x^2$ $\frac{dy}{dx} = -\frac{3}{2}x^{-2} - x$ $= -\frac{3}{2x^2} - x$	✓ $\frac{3}{2}x^{-1}$ ✓ $-\frac{3}{2}x^{-2}$ ✓ $-x$ (3)
8.2.2	$f(x) = (7x+1)^2$ $= 49x^2 + 14x + 1$ $f'(x) = 98x + 14$ $f'(1) = 98(1) + 14$ $= 112$ <p style="border: 1px solid black; padding: 5px;"> Note: Incorrect notation in 8.2.1 and/or 8.2.2: Penalise 1 mark </p> <p>OR</p> $f(x) = (7x+1)^2$ $f'(x) = 2(7x+1)(7) \text{ By the chain rule}$ $f'(x) = 98x + 14$ $f'(1) = 98(1) + 14$ $= 112$	✓ multiplication ✓ 98x ✓ 14 ✓ answer (4) ✓✓ chain rule ✓✓ answer (4) [12]

QUESTION 9

<p>9.1</p> $\begin{aligned}f(x) &= -2x^3 + ax^2 + bx + c \\f'(x) &= -6x^2 + 2ax + b \\&= -6(x-5)(x-2) \\&= -6(x^2 - 7x + 10) \\&= -6x^2 + 42x - 60\end{aligned}$ $\begin{aligned}2a &= 42 \\a &= 21 \\b &= -60\end{aligned}$ $\begin{aligned}f(5) &= -2(5)^3 + 21(5)^2 - 60(5) + c & f(2) &= -2(2)^3 + 21(2)^2 - 60(2) + c \\18 &= -25 + c & \text{OR } -9 &= -52 + c \\c &= 43 & c &= 43\end{aligned}$	<p>Note: A candidate who substitutes the values of a, b and c into the function i.e. gets $f(x) = -2x^3 - 21x^2 - 60x + 43$ and then shows by substitution that $T(2; -9)$ and $S(5; 18)$ are on the curve and works out the derivative i.e. gets $f'(x) = -6x^2 - 42x - 60$ and shows (by substitution into the derivative) that the turning points are at $x = 2$ and $x = 5$ (assuming what s/he sets out to prove and proving what is given): award max 4/7 marks as follows:</p> <ul style="list-style-type: none"> $\checkmark x = 2$ from $f'(x) = 0$ OR subs $x = 2$ into the derivative and gets 0 $\checkmark x = 5$ from $f'(x) = 0$ OR subs $x = 5$ into the derivative and gets 0 \checkmark substitution of $x = 2$ in f and gets -9 \checkmark substitution of $x = 5$ in f and gets 18 	<p>$\checkmark f'(x) = -6x^2 + 2ax + b$ $\checkmark f'(2) = 0$ $\checkmark f'(5) = 0$ $\checkmark 6a = 126$ $\checkmark b = -60$ $\checkmark \text{subs } (5; 18) \text{ or } (2; -9)$ $\checkmark c = 43$</p> <p>(7)</p>
<p>OR</p> $\begin{aligned}f'(x) &= -6x^2 + 2ax + b \\f'(2) &= -6(2)^2 + 2a(2) + b \\0 &= -24 + 4a + b \\b &= 24 - 4a \\f'(5) &= -6(5)^2 + 2a(5) + b \\0 &= -150 + 10a + b \\0 &= -150 + 10a + (24 - 4a) \\0 &= -126 + 6a \\6a &= 126 \\a &= 21 \\b &= -60\end{aligned}$ $\begin{aligned}f(5) &= -2(5)^3 + 21(5)^2 - 60(5) + c & f(2) &= -2(2)^3 + 21(2)^2 - 60(2) + c \\18 &= -25 + c & \text{OR } -9 &= -52 + c \\c &= 43 & c &= 43 \\a &= 21; b = -60; c = 43 & &\end{aligned}$	<p>Note: If derivative equal to zero is not written: penalize once only</p>	<p>$\checkmark f'(x) = -6x^2 + 2ax + b$ $\checkmark f'(2) = 0$ $\checkmark f'(5) = 0$ $\checkmark 6a = 126$ $\checkmark b = -60$ $\checkmark \text{subs } (5; 18) \text{ or } (2; -9)$ $\checkmark c = 43$</p>





OR

$$f(2) = -9 \text{ i.e. } -16 + 4a + 2b + c = -9$$

$$4a + 2b + c = 7$$

$$f(5) = 18 \text{ i.e. } -250 + 25a + 5b + c = 18$$

$$25a + 5b + c = 268$$

$$21a + 3b = 261$$

$$f'(x) = -6x^2 + 2ax + b \text{ and } f'(2) = 0 \quad \text{OR} \quad f'(5) = 0$$

$$4a + b = 24$$

$$10a + b = 150$$

$$12a + 3b = 72$$

$$9a = 189$$

$$a = \frac{189}{9}$$

$$a = 21$$

$$30a + 3b = 450$$

$$9a = 189$$

OR

$$a = \frac{189}{9}$$

$$a = 21$$

$$12(21) + 3b = 72$$

$$3b = -180$$

$$b = -60$$

$$4a + 2b + c = 7$$

$$25a + 5b + c = 268$$

$$4(21) + 2(-60) + c = 7 \quad \text{OR} \quad 25(21) + 5(-60) + c = 268$$

$$c = 43$$

$$c = 43$$

$$\checkmark -16 + 4a + 2b + c = -9 \\ \text{and } -250 + 25a + 5b + c = 18$$

$$\checkmark f'(x) = -6x^2 + 2ax + b$$

$$\checkmark f'(2) = 0 \text{ or } f'(5) = 0$$

$$\checkmark 9a = 189$$

$$\checkmark b = -60$$

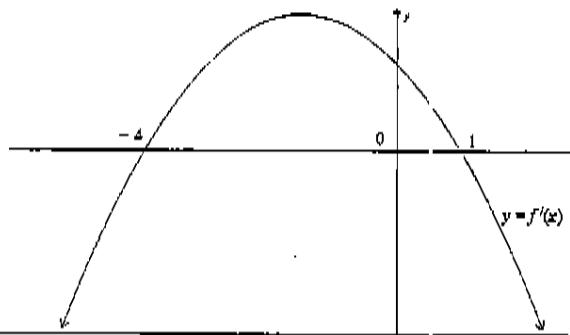
$$\checkmark \text{ subs } (5 ; 18) \text{ or } (2 ; -9)$$

$$\checkmark c = 43$$

(7)

9.2	$f'(x) = -6x^2 + 42x - 60$ $m_{\tan} = -6(1)^2 + 42(1) - 60$ $= -24$ $f(1) = -2(1)^3 + 21(1)^2 - 60(1) + 43$ $= 2$ Point of contact is $(1 ; 2)$	$y = -24x + c$ $2 = -24(1) + c$ $c = 26$ $y = -24x + 26$	$\checkmark f'(x) = -6x^2 + 42x - 60$ $\checkmark \text{ subs } f'(1)$ $\checkmark m_{\tan} = -24$ $\checkmark f(1) = 2$
9.3	$f'(x) = -6x^2 + 42x - 60$ $f''(x) = -12x + 42$ $0 = -12x + 42$ $x = \frac{7}{2}$ OR	$y = -24x + 26$	$\checkmark f''(x) = -12x + 42$ $\checkmark x = \frac{7}{2}$ $\checkmark x = \frac{2+5}{2}$

$x = \frac{2+5}{2}$ $x = \frac{7}{2}$ <p>OR</p> $x = \frac{-21}{3(-2)}$ $= \frac{7}{2}$	$\checkmark x = \frac{7}{2}$ $\checkmark x = \frac{-21}{3(-2)}$ $\checkmark x = \frac{7}{2}$ (2) [14]
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QUESTION 10

10.1	x-value of turning point: $x = \frac{-4+1}{2}$ $= -\frac{3}{2}$ $\therefore x > -\frac{3}{2}$ OR $\therefore x \in \left(-\frac{3}{2}; \infty\right)$	$\checkmark x > -\frac{3}{2}$ OR $\left(-\frac{3}{2}; \infty\right)$ (1)
10.2	f has a local minimum at $x = -4$ because: <p>OR</p> <p>$f'(x) < 0$ for $x < -4$, so f is decreasing for $x < -4$. $f'(x) > 0$ for $-4 < x < 1$, so f is increasing for $-4 < x < 1$.</p> <p>i.e. </p> <p>$\therefore f$ has a local minimum at $x = -4$</p>	$\checkmark x = -4$ \checkmark graph (3)

	OR Gradient of f changes from negative to positive at $x = -4$	$\checkmark x = -4$ \checkmark gradient negative for $x < -4$ \checkmark gradient positive for $-4 < x < 1$ (3)
	OR $f'(-4) = 0$ $f''(-4) > 0$ so graph is concave up at $x = -4$, so f has a local minimum at $x = -4$.	$\checkmark f'(-4) = 0$ $\checkmark f''(-4) > 0$ $\checkmark x = -4$ (3) [4]

QUESTION 11

11.1	$V(0) = 100 - 4(0)$ = 100 litres	\checkmark answer (1)
11.2	Rate in - rate out $= 5 - k$ l/min $V'(t) = -4$ l/min	$\checkmark 5 - k$ $\checkmark -4$ \checkmark units stated once (3)
11.3	$5 - k = -4$ $k = 9$ l/min OR Volume at any time t = initial volume + incoming total - outgoing total $100 + 5t - kt = 100 - 4t$ $5t - kt = -4t$ $9t - kt = 0$ $t(9 - k) = 0$ At 1 minute from start, $t = 1$, $9 - k = 0$, so $k = 9$	$\checkmark 5 - k = -4$ $\checkmark k = 9$ (2) Note: Answer only: award 2/2 marks $\checkmark 100 + 5t - kt = 100 - 4t$ $\checkmark k = 9$ (2)
	 OR Since $\frac{dV}{dt} = -4$, the volume of water in the tank is decreasing by 4 litres every minute. So k is greater than 5 by 4, that is, $k = 9$.	$\checkmark \checkmark k = 9$ (2) [6]

QUESTION 12

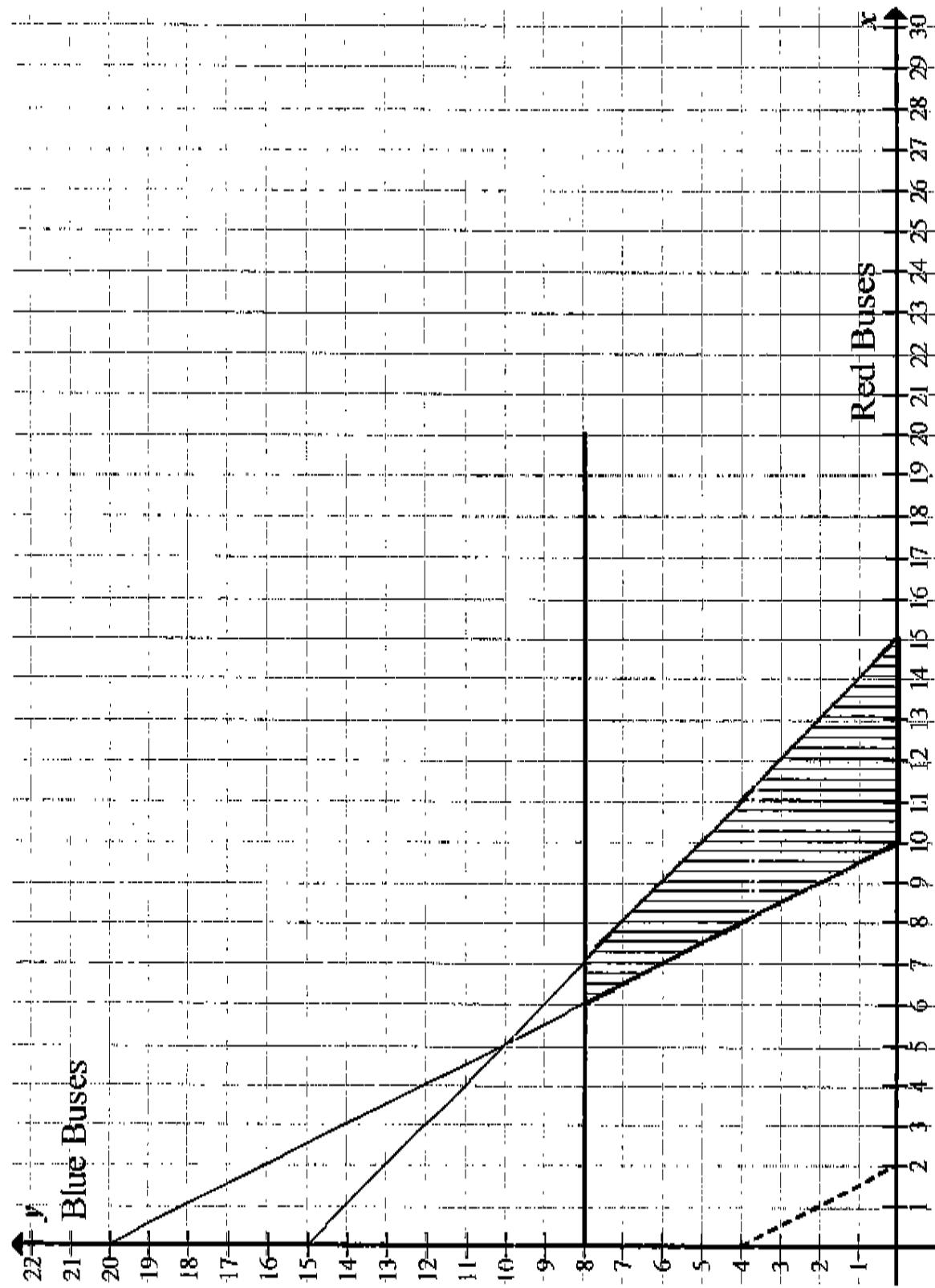
Note: If the wrong inequality $50x + 25y \leq 500$ is used, candidate wrongly says that there are more learners than available seats. Maximum of 10 marks.

12.1	$x, y \in \mathbb{N}$ $x + y \leq 15$ $50x + 25y \geq 500$ $y \leq 8$ <p style="text-align: center;">OR</p> $y \leq -x + 15$ $y \geq -2x + 20$ $y \leq 8$	<p>Note: If candidate gives $50x + 25y = 500$: max 5/6 marks</p> <p>Note: for the inequality's marks to be awarded, the LHS and the RHS must be correct</p>	✓✓ $x + y \leq 15$ ✓✓ $y \leq 8$ ✓✓ $50x + 25y \geq 500$
12.2		✓ $x + y \leq 15$ ✓ $50x + 25y \geq 500$ ✓ $y \leq 8$ ✓ feasible region	(4)
12.3	$C = 600x + 300y$	✓ answer	(1)
12.4.1	$(6 ; 8) ; (7 ; 6) ; (8 ; 4) ; (9 ; 2)$ and $(10 ; 0)$ NOTE: The gradient of the search line is $m = -\frac{2}{1}$	3 marks for all correct solutions 2 marks if only 3 or 4 correct solutions 1 mark if only 1 or 2 correct solutions	(3)
12.4.2	$C = 6(600) + 8(300) = \text{R}6\,000$ or $C = 7(600) + 6(300) = \text{R}6\,000$ or $C = 8(600) + 4(300) = \text{R}6\,000$ or $C = 9(600) + 2(300) = \text{R}6\,000$ or $C = 10(600) + 0(300) = \text{R}6\,000$	✓ subs ✓ answer	(2)
12.5	8 red ; 4 blue	✓ answer	(1)
			[17]

TOTAL: 150

*MS**PP**M 140*
Please turn over

QUESTION 12.2

*M.S.**AP 12/10/08*